



# LECTURE 13

JDR-M

# FOR TODAY

- Entrance game
- Why does Backwards Induction make sense?
- Regulation as a barrier to entry.

# MOTIVATION

- Until now, the number of producers is given
- But firms enter and exit industries every day
- Today I present the existence of equilibria with non-credible threats
- The game is the “Entrance Deterrence Model”

# ENVIRONMENT

- Players: An incumbent and an entrant
- Actions:
  - i. Entrant: enter the market (E) or not (N)
  - ii. Incumbent: Accommodate (A) (compete in a Cournot model), Price War (W) (Bertrand Competition)

# PAYOFF MATRIX ( $0 < \eta < \pi_C < \pi_M$ )

| (Incumbent, Entrant) |   | Entrant                 |              |
|----------------------|---|-------------------------|--------------|
|                      |   | E                       | N            |
| Incumbent            | A | $(\pi_C, \pi_C - \eta)$ | $(\pi_M, 0)$ |
|                      | W | $(0, -\eta)$            | $(\pi_M, 0)$ |

# STRATEGY

- Incumbent: an action  $\sigma_I \in \{A, W\}$
- Entrant: an action  $\sigma_E \in \{E, N\}$
- Strategy profile is a pair  $\sigma = (\sigma_I, \sigma_E)$

# ENTRANT'S PROBLEM

- Assuming an incumbent action  $\sigma_I$ , entrant solves

$$(1) \pi_E(\sigma_I) = \max_{a \in \{E, N\}} 1_{a=E} (1_{\sigma_I=A} (\pi_C - \eta) - \eta 1_{\sigma_I=W})$$

# INCUMBENT'S PROBLEM

- Assuming an entrant action  $\sigma_E$ , the Incumbent solve

$$(2) \pi_I(\sigma_E) = \max_{a \in \{W, A\}} 1_{\sigma_E=N} \pi_M + 1_{\sigma_E=A} 1_{a=A} \pi_C$$



# EQUILIBRIUM

- An Equilibrium is a strategy profile  $\sigma = (\sigma_E, \sigma_I)$  such that
  - i. Given  $\sigma_I, \sigma_E$  solves (1)
  - ii. Given  $\sigma_E, \sigma_I$  solves (2)

# CHARACTERIZATION 1

- There exists 2 equilibria.
- Equilibrium 1: Suppose that the Incumbent expects the entrant to enter the market, then he faces the problem

$$(3) \pi_I(E) = \max_{a \in \{W, A\}} 1_{a=A} \pi_C$$

- Since  $\pi_C > 0$ , the incumbent chooses  $\sigma_I = A$

## CHARACTERIZATION 2

- Suppose that the entrant expects that incumbent plays A, then he faces the problem

$$(4) \pi_E(A) = \max_{a \in \{E, N\}} 1_{a=E}(\pi_C - \eta)$$

- Since  $\pi_C > \eta$ , then the incumbent chooses  $\sigma_E = E$
- These two problems show that  $\sigma = (E, A)$  is an equilibrium as each player does as described in the tuple when they expect their peers to also follow what it's stated in the tuple

# CHARACTERIZATION 3

- Q: Is this the only equilibrium?
- A: No.
- Suppose that incumbent expects  $\sigma_E = N$ , then he faces the problem

$$(5) \pi_I(N) = \max_{a \in \{W, A\}} 1_{a=A} \pi_M + 1_{a=W} \pi_M$$

- Observe that the incumbent is indifferent between either action, so he could choose  $\sigma_I = W$

# CHARACTERIZATION 4

- Suppose that the entrant expects the seller to play  $W$ , then his problem becomes

$$(6) \pi_E(W) = \max_{a \in \{E, N\}} -1_{a=E} \eta$$

- Since  $\eta > 0$ , the entrant prefers not entering, thus  $\sigma_E = N$
- Therefore,  $\sigma = (N, W)$  is ALSO AN EQUILIBRIUM.

# PUNCHLINE

- When we do not model the timing in this game, we have two equilibrium
- $(E, A)$  makes sense, but  $(N, W)$  seems weird
- The first equilibrium states that the entrant Enters and the incumbent prefers to accommodate rather than lose profits in order to punish the entrant
- The second states that the entrant stays away expecting the incumbent to start a price war and the incumbent keeps his promise.

# ADDING A TIMING

- Suppose that the timing is the following:
  1. Entrant makes his decision and the Incumbent observes his action
  2. Incumbent makes his choice.

# STRATEGIES

- An entrant strategy is  $\sigma_E \in \{E, N\}$
- An incumbent strategy is a function  $\sigma_I: \{E, N\} \rightarrow \{A, W\}$



# EQUILIBRIUM

- An equilibrium is a strategy profile  $\sigma = (\sigma_E, \sigma_I)$  such that
  - i. Conjecturing an incumbent strategy  $\sigma_I, \sigma_E$  solves (1)
  - ii. For each observed action  $a \in \{E, N\}$ , choice  $\sigma_I(a)$  solves (2)

# CHARACTERIZATION 1

- This equilibrium can be characterized via Backwards Induction
- First, the incumbent's strategy solves the same problems as before and his optimal strategy is

$$(7) \sigma_I(a) = \begin{cases} iA & \text{if } a = E \\ \tilde{\sigma} \in \{A, W\} & \text{if } a = N \end{cases}$$

## CHARACTERIZATION 2

- The entrant rightly conjecturing potential incumbent strategies expects to be accommodated provided that he enters the market, so he picks  $\sigma_E = E$ .
- All equilibrium are then payoff equivalent to  $\sigma = (E, (\sigma_I(E) = A, \sigma_I(N) = W))$

# PUNCHLINE

- When one adds a timing of play, we can eliminate a “weird” equilibrium
- Q: Can one change the game in play such that the sole equilibrium is the “weird” equilibrium?
- A: Yes!

# ENTRY GAME WITH STACKELBERG OR COURNOT COMPETITION

- Players: An incumbent and an entrant
- Actions:
  - i. Entrant: enter the market (E) or not (N)
  - ii. Incumbent: Wait (W), Stackelberg quantity (S)

PAYOFF MATRIX ( $0 < \pi_2^S \leq \eta < \pi_C < \pi_1^S < \pi_M$ )

| (Incumbent, Entrant) |   | Entrant                     |              |
|----------------------|---|-----------------------------|--------------|
|                      |   | E                           | N            |
| Incumbent            | W | $(\pi_C, \pi_C - \eta)$     | $(\pi_M, 0)$ |
|                      | S | $(\pi_1^S, \pi_2^S - \eta)$ | $(\pi_M, 0)$ |

# TIMING

- We can define strategies and equilibrium for this game
- Characterizing these equilibria leads us to 2 equilibria:  $(S, N)$
- Next, assume that the timing is the following
  1. Incumbent decides to pick his Stackelberg quantity or to wait for the entrant
  2. Entrant either stays away or enters and picks a quantity to produce

# EQUILIBRIUM AND INSIGHT

- The equilibrium can be defined and characterized but the only equilibrium we get is  $\sigma = (S, (\sigma_E(S) = N, \sigma_E(W) = N))$
- Therefore, we learn several things
  1. Who makes a choice first matters
  2. Changing the threat, changes the prediction
  3. The cost of entrance matter: large entrance cost ( $\eta > 0$ ), the less likely one gets entry
  4. Real world ways to get higher entrance costs includes increasing regulatory costs.